EBERHARD KANIUTH, University of Paderborn, 33095 Paderborn, Germany Stable rank and real rank of group  $C^*$ -algebras

The stable rank and the real rank of a  $C^*$ -algebra A have been introduced by Rieffel and Brown and Pedersen, respectively, as non-commutative analogues of the complex and the real dimension of topological spaces. In fact, for the algebra of continuous functions on a compact Hausdorff space X one has  $RR(C(X)) = \dim X$  and a similar formula for sr(C(X)). Both of these ranks (in particular the condition RR(A) = 0) have played a significant role in the classification of  $C^*$ -algebras, and there is now an extensive literature available, especially on group  $C^*$ -algebras. The talk will focus on recent work with R. J. Archbold (Aberdeen, Scotland) and will discuss formulæ for the ranks of group  $C^*$ -algebras  $C^*(G)$  for various classes of locally compact groups G, such as nilpotent groups, motion groups and crystal groups.