
PETER DANZIGER, Toronto Metropolitan University

Packing designs with large block size

Given positive integers v, k, t and λ with $v \geq k \geq t$, a packing design $\text{PD}_\lambda(v, k, t)$ is a pair $(V, \mathcal{B})$, where V is a v -set and $\mathcal{B}$ is a collection of k -subsets of V such that each t -subset of V appears in at most λ elements of $\mathcal{B}$. When $\lambda = 1$, a $\text{PD}_1(v, k, t)$ is equivalent to a binary code with length v , minimum distance $2(k - t + 1)$ and constant weight k . The maximum size of a $\text{PD}_\lambda(v, k, t)$ is called the packing number, denoted $\text{PDN}_\lambda(v, k, t)$.

We consider packing designs with k large relative to v . In this case, we extend the second Johnson bound to arbitrary λ and show that this bound is tight. Specifically, we prove that for a positive integer n , $\text{PDN}_\lambda(v, k, t) = n$ whenever $nk - (t - 1)\binom{n}{\lambda+1} \leq \lambda v < (n + 1)k - (t - 1)\binom{n+1}{\lambda+1}$. For fixed t and λ , this determines the value of $\text{PDN}_\lambda(v, k, t)$ when k is large with respect to v . We also extend this result to directed packings, by showing that if no point appears in more than three blocks, then the blocks of a $\text{PD}_2(v, k, 2)$ can be directed so that no ordered pair occurs more than once.

Joint work with Andrea Burgess, Daniel Horsley and Muhammad Tariq Javed