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A shape theorem for the convex hull of d -dimensional branching Brownian motion in periodic environments.

We consider the long-time behaviour of a "heterogeneous" binary branching Brownian motion (BBM) in which the branching rate depends on where the branching event occurs. More precisely, for a positive function g , the instantaneous branching rate of a particle at location x is characterized by $g(x)$ (we refer to this as g -BBM). When g is periodic, we expect that the microscopic effects of g average out on large scales, and the process should exhibit asymptotically homogeneous behaviour. Nevertheless, the heterogeneity of the branching rate introduces new technical challenges.

In this talk, I will prove a shape theorem for the convex hull of the g -BBM in all dimensions, namely that there exists a deterministic set \mathcal{W} such that almost surely as $t \rightarrow \infty$, the convex hull of the g -BBM approximates $t\mathcal{W}$. This talk is based on joint work in progress with Louigi Addario-Berry (McGill) and Jessica Lin (McGill).