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Bollobas-Nikiforov conjecture and triangle counting

Let G be a graph with n vertices. Let A(G) be its adjacency matrix. Let $\lambda_1(G), \lambda_2(G)$ denote the largest and second largest eigenvalues of the adjacency matrix. Bollobás and Nikiforov (2007) conjectured that for any graph $G \neq K_n$ with m edges

$$\lambda_1^2 + \lambda_2^2 \leq \bigg(1 - \frac{1}{\omega(G)}\bigg) 2m$$

where $\omega(G)$ denotes the clique number of G. In this talk, we prove this conjecture for graphs with not so many triangles, using the method of triangle counting. This is a joint work with Hitesh Kumar.