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Least Wasserstein Distance Between Disjoint Shapes With Perimeter Regularization

We prove the existence of global minimizers to the double minimization problem

$$\inf \left\{ P(E) + \lambda W_p(\mathcal{L}^n \lfloor E, \mathcal{L}^n \lfloor F) \colon |E \cap F| = 0, \, |E| = |F| = 1 \right\},\$$

where P(E) denotes the perimeter of the set E, W_p is the p-Wasserstein distance between Borel probability measures, and $\lambda > 0$ is arbitrary. The result holds in all space dimensions, for all $p \in [1, \infty)$, and for all positive λ . This answers a question of Buttazzo, Carlier, and Laborde.