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Sign changes of the error term in the Piltz divisor problem
For an integer $k \geq 3$, let $\Delta_{k}(x):=\sum_{n \leq x} d_{k}(n)-\operatorname{Res}_{s=1}\left(\zeta^{k}(s) x^{s} / s\right)$, where $d_{k}(n)$ is the $k$-fold divisor function and $\zeta(s)$ is the Riemann zeta-function. In the 1950 's, Tong showed for all large enough $X$ that $\Delta_{k}(x)$ changes sign at least once in the interval $\left[X, X+C_{k} X^{1-1 / k}\right]$, where $C_{k}$ is some constant. Assuming the Lindelof Hypothesis, we show the existence of many subintervals of $[X, 2 X]$ of length $X^{1-1 / k-\varepsilon}$ such that $\Delta_{k}(x)$ does not change sign in any of these subintervals. This is joint work with Cruz Castillo.

