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Rational points on algebraic curves in infinite towers of number fields

We study a natural question in the Iwasawa theory of algebraic curves of genus > 1.

Let X be a smooth, projective, geometrically irreducible curve X defined over a number field K of genus g > 1, such that the Jacobian has good ordinary reduction at the primes above p. Fix an odd prime p and for any integer n > 1, let K_n denote the degree- p^n extension of K contained in $K(\mu_{p^{n+1}})$. We prove explicit results for the growth of $\#X(K_n)$ as $n \to \infty$. When the Jacobian of X has rank zero and the associated adelic Galois representation has big image, we prove an explicit condition under which $X(K_n) = X(K)$ for all n. We show that this condition is satisfied for 100% of primes p at which the Jacobian of X has good ordinary reduction.