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Rational points on algebraic curves in infinite towers of number fields
We study a natural question in the Iwasawa theory of algebraic curves of genus $>1$.
Let $X$ be a smooth, projective, geometrically irreducible curve $X$ defined over a number field $K$ of genus $g>1$, such that the Jacobian has good ordinary reduction at the primes above $p$. Fix an odd prime $p$ and for any integer $n>1$, let $K_{n}$ denote the degree- $p^{n}$ extension of $K$ contained in $K\left(\mu_{p^{n+1}}\right)$. We prove explicit results for the growth of $\# X\left(K_{n}\right)$ as $n \rightarrow \infty$. When the Jacobian of $X$ has rank zero and the associated adelic Galois representation has big image, we prove an explicit condition under which $X\left(K_{n}\right)=X(K)$ for all $n$. We show that this condition is satisfied for $100 \%$ of primes $p$ at which the Jacobian of $X$ has good ordinary reduction.

