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The radius of comparison of the crossed product by a tracially strictly approximately inner action

Let G be a finite group, let A be an infinite-dimensional stably finite simple unital C*-algebra, and let $\alpha\colon G \to \mathrm{Aut}(A)$ be a tracially strictly approximately inner action of G on A. Then the radius of comparison satisfies $\mathrm{rc}(A) \leq \mathrm{rc}\left(A \rtimes_{\alpha} G\right)$ and if $A \rtimes_{\alpha} G$ is simple, then $\mathrm{rc}(A) \leq \mathrm{rc}\left(A \rtimes_{\alpha} G\right) \leq \mathrm{rc}(A^{\alpha})$.

Also, for every finite group G and for every $\eta \in \left(0, \frac{1}{\mathrm{card}(G)}\right)$, we construct a simple separable unital AH algebra A with stable rank one and a strictly approximately inner action $\alpha\colon G \to \mathrm{Aut}(A)$ such that:

(1) α is pointwise outer and doesn't have the weak tracial Rokhlin property.

(2) $\mathrm{rc}(A) = \mathrm{rc}\left(A \rtimes_{\alpha} G\right) = \eta$.