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**DILIAN YANG**, University of Windsor  
*Zappa-Szép Actions of Groups on Product Systems*

Let  $G$  be a group and  $X$  be a product system over a semigroup  $P$ . Suppose  $G$  has a left action on  $P$  and  $P$  has a right action on  $G$ , so that one can form a Zappa-Szép product  $P \bowtie G$ . We define a *Zappa-Szép action* of  $G$  on  $X$ , roughly speaking, to be a collection of functions on  $X$ , which is compatible with both actions from  $P \bowtie G$ . For a given Zappa-Szép action of  $G$  on  $X$ , we construct a new product system  $X \bowtie G$  over  $P \bowtie G$ , which is called the Zappa-Szép product of  $X$  by  $G$ . Then we associate  $X \bowtie G$  some universal  $C^*$ -algebras, and show some Hao-Ng type isomorphisms. A special case of interest is when the action is homogenous.

This is ongoing joint work with Boyu Li.