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Derivatives of L-series and generalized Stieltjes constants

Generalized Stieltjes constants occur as coefficients of $(s-1)^k$ in the Laurent series expansion of certain Dirichlet series around s = 1. The connection between these generalized Stieltjes constants and derivatives of L(s, f) for periodic arithmetical functions f, at s = 1 is known. We utilize this link to throw light on the arithmetic nature of L'(1, f) and certain Stieltjes constants. In particular, if p is an odd prime greater than 7, then we deduce the transcendence of at least (p-7)/2 of the generalized Stieltjes constants, $\{\gamma_1(a, p) : 1 \le a < p\}$, conditional on a conjecture of S. Gun, M. Ram Murty and P. Rath.