Let $r_5(n)$ be the number of ways of writing n as a sum of five integer squares. In his study of this function, Bateman was led to formulate a conjecture regarding the sum

$$\sum_{|j| \le \sqrt{n}} \sigma(n - j^2)$$

where $\sigma(n)$ is the sum of positive divisors of n. We give a proof of Bateman's conjecture in the case n is square-free and congruent to 1 (mod 4). This is joint work with Prof. Ram Murty (Queen's University).

ARPITA KAR, Queen's University, Kingston, Canada On a Conjecture of Bateman about $r_5(n)$