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Comparing skew Schur functions: a quasisymmetric perspective
This story begins with work of Reiner, Shaw and van Willigenburg, where they showed that if two skew Schur functions $s_{A}$ and $s_{B}$ are equal, then the skew shapes $A$ and $B$ must have the same "row overlap partitions." Unfortunately, the converse is not true. Recently, we have shown that these row overlap equalities are also implied by a much weaker condition than skew Schur equality: that $s_{A}$ and $s_{B}$ have the same support when expanded in the fundamental quasisymmetric basis $F$. Surprisingly, there is significant evidence supporting a conjecture that the converse is also true.
In fact, we will work in terms of inequalities: if the $F$-support of $s_{A}$ contains that of $s_{B}$, then the row overlap partitions of $A$ are dominated by those of $B$. Again, we conjecture that the converse also holds. After giving evidence in favor of our conjecture, we will conclude with a consideration of how the quasisymmetric Schur basis and the dual immaculate basis fit into our framework.

