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Sporadic Reinhardt polygons

Let n be a positive integer, not a power of two. A *Reinhardt polygon* is a convex n -gon that is optimal in three different geometric optimization problems: it has maximal perimeter relative to its diameter, maximal width relative to its diameter, and maximal width relative to its perimeter. There is a correspondence between Reinhardt polygons and polynomials with specific divisibility properties and with tight restrictions on their coefficients. This correspondence is useful in the construction of such polygons. For almost all n , there are many Reinhardt polygons with n sides, and many of them exhibit a particular periodic structure. While these periodic polygons are well understood, for certain values of n , additional Reinhardt polygons exist that do not possess this structured form. We call these polygons *sporadic*. We completely characterize the integers n for which sporadic Reinhardt polygons exist, showing that these polygons occur precisely when $n = pqr$ with p and q distinct odd primes and $r \geq 2$. We also prove that a positive proportion of the Reinhardt polygons with n sides are sporadic for almost all integers n , and we investigate the precise number of sporadic Reinhardt polygons that are produced for several values of n by a construction that we introduce.