
THOMAS BRÜSTLE, Université de Sherbrooke and Bishop's University
Projective dimension of modules over cluster-tilted algebras

In joint work with Louis Beaudet and Gordana Todorov we study the projective dimension of modules over a cluster-tilted algebra $\text{End}(T)$ where T is a tilting object in a cluster category \mathcal{C} . It is well-known that all modules are of the form $\text{Hom}(T, M)$ for some object M in \mathcal{C} , and since $\text{End}(T)$ is Gorenstein of dimension 1, the projective dimension of $\text{Hom}(T, M)$ is either zero, one or infinity.

We consider the ideal I_M of $\text{End}_{\mathcal{C}}(T[1])$ given by all endomorphisms that factor through M , and show that the $\text{End}(T)$ -module $\text{Hom}(T, M)$ has infinite projective dimension precisely when I_M is non-zero. Examples indicate that the objects M of \mathcal{C} such that $I_M \neq 0$ lie on hammocks in \mathcal{C} .