
OLIVIER COLLIN, Université du Québec à Montréal

Non-trivial actions on Floer homology

Given a finite order orientation-preserving diffeomorphism $\tau: Y^3 \rightarrow Y^3$ of an integer homology sphere Y^3 , it is an interesting and difficult general problem to understand the effect of the induced map on instanton Floer homology. In this talk, we consider odd-order diffeomorphisms of integer homology sphere and their induced effect on $SU(2)$ -character varieties and Floer homology. We are interested in cases where the resulting equivariant Casson invariant differs from the Casson and the consequences for finding non-trivial actions on Floer homology. This provides the first examples of non-trivial odd-order actions on the Floer homology of irreducible homology spheres. We shall also see how this can be related to the existence of incompressible surfaces in the 3-manifold Y^3 .