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Bethe subalgebras of the Yangian $Y(\mathfrak{gl}(n))$, tame representations, and Gelfand-Tsetlin patterns

The Bethe subalgebras of the Yangian $Y(\mathfrak{gl}(n))$ form a family of maximal commutative subalgebras indexed by points of the Deligne-Mumford compactification of the moduli space $M(0, n+2)$. When considering a point C in the real locus of this parameter space, the corresponding Bethe subalgebra $B(C)$ acts with simple spectrum on a given tame representation of $Y(\mathfrak{gl}(n))$. This results in an unramified covering, whose fiber over C is the set of eigenlines for the action of $B(C)$. I will discuss the identification of each fiber with a collection of Gelfand-Tsetlin keystone patterns, which carry a $\mathfrak{gl}(n)$ -crystal structure, as well as the monodromy action realized by a type of cactus group. This is joint work with Anfisa Gurenkova and Leonid Rybnikov.