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*Cohomological Duality in the Local Langlands Correspondence for  $p$ -adic Groups*

The Langlands Programme seeks to classify the irreducible representations of a connected, reductive algebraic group  $G$  over a field  $k$ , roughly in correspondence with the representations of  $\text{Gal}(\bar{k}/k)$ , deemed  $L$ -parameters. For local fields, this classification has largely been a success, and a natural next step is to classify the extensions between these irreducible representations of  $G$ . In this talk, we show that, for  $G$  split semisimple over a  $p$ -adic field, certain classes of extensions can be classified according to the extensions of perverse sheaves on a moduli space built from the  $L$ -parameters.