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*Space-time HDG for the advection-diffusion equation on time-dependent domains in the limit of small diffusion*

This work is in collaboration with Yuan Wang. The time-dependent advection-diffusion equation on a time-dependent domain  $D(t) \subset \mathbb{R}^d$  is given by:

$$\partial_t \theta + \mathbf{u} \cdot \nabla \theta - \nu \nabla^2 \theta = f, \quad \mathbf{x} \in D(t), \quad t \in (0, T]. \quad (1)$$

Here  $\theta$  is the quantity of interest,  $\mathbf{u}$  is a flow field, and  $\nu > 0$  a diffusion parameter.

The space-time framework facilitates the discretization of PDEs on moving domains: a time-dependent PDE is re-formulated as a “stationary” PDE in  $(d + 1)$  space-time which is then discretized by a finite element method.

In [1] we introduced the space-time hybridizable discontinuous Galerkin method for (1). In [2] we analyzed this discretization assuming a sufficiently large diffusion parameter  $\nu$ . In this talk I will present a new analysis of the space-time HDG method focusing on the small diffusion limit ( $\nu \ll 1$ ).

[1] S. Rhebergen and B. Cockburn, Space-time hybridizable discontinuous Galerkin method for the advection-diffusion equation on moving and deforming meshes, in *The Courant-Friedrichs-Lewy (CFL) condition, 80 years after its discovery*, ed. C.A. de Moura and C.S. Kubrusly, pp. 45-63 (2013).

[2] K.L.A. Kirk, T. Horvath, A. Cesmelioglu and S. Rhebergen, Analysis of a space-time hybridizable discontinuous Galerkin method for the advection-diffusion problem on time-dependent domains, *SIAM J. Numer. Anal.*, 57, 4, pp. 1677-1696 (2019).