ELISABETH WERNER, Case Western Reserve University
On the geometry of projective tensor products
We study the volume ratio of the projective tensor products $\ell_{p}^{n} \otimes_{\pi} \ell_{q}^{n} \otimes_{\pi} \ell_{r}^{n}$ with $1 \leq p \leq q \leq r \leq \infty$. We obtain asymptotic formulas that are sharp in almost all cases. As a consequence of our estimates, these spaces allow a nearly Euclidean decomposition of Kashin type whenever $1 \leq p \leq q \leq r \leq 2$ or $1 \leq p \leq 2 \leq r \leq \infty$ and $q=2$. Also, from the Bourgain-Milman bound on the volume ratio of Banach spaces in terms of their cotype 2 constant, we obtain information on the cotype of these 3 -fold projective tensor products. Our results naturally generalize to $k$-fold products $\ell_{p_{1}}^{n} \otimes_{\pi} \cdots \otimes_{\pi} \ell_{p_{k}}^{n}$ with $k \in \mathbb{N}$ and $1 \leq p_{1} \leq \cdots \leq p_{k} \leq \infty$.
Based on joint work with O. Giladi, J. Prochno, C. Schuett and N. Tomczak-Jaegermann.

