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Prescribing the radial limits of solutions to a PDE

Let S^{n-1} be the unit sphere in \mathbb{R}^n , and (θ, r) be the polar representation of points in \mathbb{R}^n , for $\theta \in S^{n-1}$, and $r \geq 0$. Moreover, let us call L -harmonic functions the solutions of the PDE $Lu = 0$.

Now, let suppose $U = (U', R)$ is a strictly starlike domain in \mathbb{R}^n , $n \geq 2$, and let F' be an F_σ subset of U' , which is of first category if $n = 2$, and polar if $n > 2$. Then, we shall introduce a class of partial differential operators L such that for every function φ continuous on U , there is a L -harmonic function h on U such that, for all $\theta \in F'$, we have

$$(h - \varphi)((\theta, r)) \rightarrow 0.$$

as (θ, r) goes to the boundary of U . That is, the radial limits of h can be prescribed by a continuous function.

This is a joint work with Paul. M. Gauthier.