
TIANYUAN XU, Queen's University

On quivers and the subregular J -rings of Coxeter systems

Let (W, S) be an arbitrary Coxeter system and let G be its Coxeter diagram. We recall Lusztig's construction of the asymptotic Hecke algebra J of (W, S) , an associative algebra closely related to the Iwahori–Hecke algebra of (W, S) , and present some results on a subalgebra J_C of J that we call the subregular J -ring. We show that while products in J are defined in terms of Kazhdan–Lusztig polynomials, they can be computed by a simple combinatorial algorithm in J_C . We also relate J_C to the path algebra of a quiver constructed from G , and use the relation to deduce some results on the representations of J_C . (Joint work with Ivan Dimitrov, Charles Paquette, and David Wehlau.)