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On the monotone properties of general affine surfaces under the Steiner symmetrization

Affine surface areas are fundamental in (affine) convex geometry and play key roles in many problems such as affine isoperimetric inequalities. The study of affine surface areas has a long history and went back to Blaschke in 1923.

Recently, general affine surface areas were introduced by Ludwig. Such general affine surface areas can involve nonhomogenous (convex and/or concave) functions, and have many nice properties, such as, affine invariance, upper-semicontinuity (or lower-simicontinuity), and valuation. Related affine isoperimetric inequalities have been proved by Ludwig via the Blaschke-Santalo inequality.

In this talk, I will introduce the concept of general affine surface areas, and prove the monotone properties of general affine surfaces under the Steiner symmetrization. As a byproduct, we provide another proof of the affine isoperimetric inequalities for general affine surface areas without assuming the Blaschke-Santalo inequality. Hence, the centroid condition (required by the Blaschke-Santalo inequality) can be removed.