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Green rings of rank one pointed Hopf algebras of nilpotent type

Let H be a finite dimensional pointed rank one Hopf algebra of nilpotent type, and G = G(H), the group of group-like elements of H. We study the finite dimensional indecomposable H-modules and establish the Clebsch-Gordan formulas for the decompositions of the tensor products of indecomposable H-modules. It turns out that the Green ring r(H) is commutative and generated by one variable over the Grothendieck ring of the group algebra kG modulo one relation. The Jacobson radical of r(H) is completely determined and is a principal ideal of r(H) generated by one element. As an example, we shall describe the Green ring of the pointed rank one Hopf algebra H with G(H) a Dihedral group.