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*weighted quadrature in Besov spaces with  $A_\infty$  weights on multivariate domains*

Let  $\Omega$  denote either the unit sphere  $S^{d-1} := \{x \in \mathbb{R}^d : \|x\| = 1\}$ , or the unit ball  $B^d := \{x \in \mathbb{R}^d : \|x\| \leq 1\}$ , or the standard simplex  $T^d := \{x \in \mathbb{R}^d : x_1, \dots, x_d \geq 0, \sum_{j=1}^d x_j \leq 1\}$ , and let  $w$  be an  $A_\infty$  weight on  $\Omega$ . For the unit ball  $MB_\tau^\alpha(L_{p,w})$  of the weighted Besov space  $B_\tau^\alpha(L_{p,w})$  on  $\Omega$ , we find the sharp asymptotic order of the following quantity as  $n \rightarrow \infty$ :

$$\inf_{\substack{\lambda_1, \dots, \lambda_n \in \mathbb{R} \\ \xi_1, \dots, \xi_n \in \Omega}} \sup_{f \in MB_\tau^\alpha(L_{p,w})} \left| \int_{\Omega} f(x)w(x) dx - \sum_{j=1}^n \lambda_j f(\xi_j) \right|.$$

We also establish a similar result on unweighted spherical caps.