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Depth of a Subgroup

A subalgebra pair of semisimple complex algebras $B \subset A$ with inclusion matrix M is depth two if $MM^tM < nM$ for some positive integer n and all corresponding entries. If A and B are the group algebras of finite group-subgroup pair $H < G$, the induction-restriction table for irreducible characters equals M , and $S = MM^t$ satisfies $S^2 < nS$ iff the subgroup H is depth three in G ; similarly depth $n > 3$ by successive right multiplications of this inequality with alternately M and M^t . For example, the pair of permutation groups $S_n < S_{n+1}$ has depth $2n - 1$ (or more). In joint work with Kuelshammer and Burciu, we show that a subgroup H has depth $2n + 2$ if its core is an intersection of H with n conjugates of H .