**JIE XIAO**, Memorial University, St. John's, NL A1C 5S7 Some Geometric Criteria for  $L^2$  Sobolev/Nash/Log-Sobolev Inequalities on Complete Noncompact Riemannian Manifolds

In this talk we will discuss certain generic and optimal geometric criteria for the mutually interacted Sobolev, Nash, logarithmic Sobolev inequalities of  $L^2$  type on  $3 \le n$ -dimensional, complete, non-compact, Riemannian manifolds. More attention is paid on those aspects connecting the volumes and the Green's functions of regular bounded open subsets of the manifolds.