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Chromatic numbers of Steiner quadruple systems

A Steiner quadruple system of order v , $\text{SQS}(v)$, is a pair (X, B) , where B is a set of 4-subsets of X such that each 3-subset of X is in a unique member of B . Hanani showed that an $\text{SQS}(v)$ exists if and only if $v = 0, 1$ or $v \equiv 2, 4 \pmod{6}$. An $\text{SQS}(v)$ is commonly described as a $S(3, 4, v)$ design, and as a 4-uniform hypergraph each $\text{SQS}(v)$ has a chromatic number.

For a given $k \geq 2$, a basic problem is to determine all v for which a k -chromatic $\text{SQS}(v)$ exists. We survey recent progress on this problem and point out avenues for future research.