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*Anti-Ramsey Thresholds*

We call an edge-coloring of a graph a  $k$ -coloring if it uses no more than  $k$  colors and  $k$ -bounded if it uses no color more than  $k$  times. We call a subgraph homogeneous if all of its edges are colored the same and heterogeneous if all of its edges are colored differently.

A classical Ramsey theorem states that for every  $k$  and  $n$  there exists an  $m$  such that any  $k$ -coloring of the edges of  $K_m$  contains a homogeneous  $K_n$ . Rodl *et al.* proved the following anti-Ramsey theorem: for every  $k$  and every  $n$  there exists an  $m$  such that any  $k$ -bounded coloring of the edges of  $K_m$  contains a heterogeneous  $K_n$ .

Let  $H$  be a fixed connected graph that contains a cycle. In this talk we establish the threshold for the property that every  $k$ -bounded coloring of the random graph  $G_{n,p}$  has a heterogeneous copy of  $H$ . We also discuss the behavior of the probability that  $G_{n,p}$  has this property for  $p$  close to the threshold and pose a conjecture for the threshold when  $H$  is a tree.

This is joint work with Alan Frieze, Oleg Pikhurko and Cliff Smyth.