CRISTIAN RIOS, University of Calgary

Continuity of solutions to infinite degenerate elliptic equations in the plane

We obtain the continuity of weak solutions to infinite degenerate quasilinear equations

$$-\operatorname{div}\mathcal{A}(x,u)\nabla u = \phi_0 - \operatorname{div}_A\vec{\phi}_1$$

where one of the eigenvalues of the elliptic matrix A is allowed to vanish to infinite order as x approaches the vertical axis. This is an application of an abstract result obtained in all dimensions $n \ge 2$. The Carnot-Carathéodory metric associated with the operator is highly non-doubling, so traditional methods have to be adapted to Orlicz-Sobolev embeddings with gains smaller than any power p > 1. In particular, our methods include the first realization of a Moser iteration technique in such infinite degenerate geometries. This work was done in collaboration with Lyudmila Korobenko, Eric Sawyer, and Ruipeng Shen.