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 $p\mbox{-}adic$  companion forms for Yoshida lifts

Coleman defined a p-adic theta operator on overconvergent forms, mapping forms of slope 0 and weight 2 - k to forms of slope k - 1 and weight k. By explicitly computing the q-expansion, he proved that the critical p-stabilization of a p-ordinary CM form lies in the image of the theta operator. The parallel statement on the Galois side is that the Galois representation of a CM form splits locally at p. Coleman and Greenberg conjectured the respective converse, but both still remain open. In the GSp<sub>4</sub> setting, the Galois representation of a Yoshida lift splits locally into two 2-by-2 blocks at p. Our goal is to prove that the critical p-stabilization of a Yoshida lift lies in the image of a relevant theta operator. With Bharathwaj Palvannan, we figured out the effect of the relevant theta operator on the q-expansion as a first step toward the goal.