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Incidence estimates for well spaced rectangles

We discuss estimating the overlap of thin rectangles in the plane in terms of how many rectangles clump together in fatter rectangles. This question can be seen as a generalization of the Szemeredi-Trotter theorem in incidence geometry, where straight lines are replaced by thin rectangles. Although the Szemeredi-Trotter theorem is sharp, there remain serious open problems involving these analogous questions for thin rectangles. We discuss a recent approach to the tube problem using Fourier analysis. This approach connects to decoupling and to the local smoothing problem for the wave equation.