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Constraint Satisfaction Problem dichotomy update

Given a finite relational structure M in a finite signature L , the Constraint Satisfaction Problem for M , or $\text{CSP}(M)$, is the decision problem which, given a primitive positive sentence in the signature of L as input, asks whether the sentence is true in M . Each such problem $\text{CSP}(M)$ is clearly in NP. The CSP Dichotomy Conjecture, dating back to work of Feder and Vardi in the 1990s, posits that for each such M , $\text{CSP}(M)$ is either in P or is NP-complete.

The Dichotomy Conjecture has (apparently) been proved by Andrei Bulatov and independently by Dmitriy Zhuk; see <https://arxiv.org/abs/1704.01914> and <https://arxiv.org/abs/1704.01914>. In this talk I will briefly describe the (known) connection of such problems to universal algebra, discuss a key component of Zhuk's proof, and indicate one way in which the proof can be strengthened.