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Solutions of certain polynomial Diophantine equations

For each integer $n \ge 1$ we consider the unique polynomials $P,Q \in \mathbb{Q}[x]$ of smallest degree n that are solutions of the equation $P(x)x^{n+1} + Q(x)(x+1)^{n+1} = 1$. We derive numerous properties of these polynomials, including explicit expansions, differential equations, recurrence relations, generating functions, discriminants, irreducibility results, and their zero distribution. We also consider some related polynomials and their properties.

(Joint work with Maciej Ulas, Jagiellonian University).