This talk is based on preprints 1910.11522 and 1810.03246.

**NICK EARLY**, Perimeter Institute for Theoretical Physics From weakly separated collections to matroid subdivisions

We study arrangements of slightly skewed tropical hyperplanes, called blades, on the vertices of a hypersimplex  $\Delta_{k,n}$ . We reformulate the condition under which such an arrangement induces a matroid (in fact a positroid) subdivision as the requirement that the collection of vertices must satisfy pairwise a certain non-crossing condition on a chord diagram: pairs of vertices should be weakly separated. This work is motivated in part by recent joint work together with Cachazo, Guevara and Mizera, where a formulation was proposed for quantum field theory over  $\mathbb{CP}^{k-1}$ .