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Geometric Fock Space Representations of Affine $sl(n)$ and $gl(n)$

Fock space has a basis naturally enumerated by Young diagrams. There exists a well-known combinatorial representation of affine $sl(n)$ on Fock space, where the Chevalley generators act by adding and removing boxes. This can be extended to an action of affine $gl(n)$, resulting in a combinatorial realization of the so-called basic representation. In this talk, we describe a geometric realization of Fock space using the equivariant cohomology of Hilbert schemes and Nakajima quiver varieties. In particular, we show how to geometrically describe the action of affine $sl(n)$ and $gl(n)$ using “geometric operators” arising from the top nonvanishing Chern classes of certain equivariant vector bundles. Our description, which is more general than those previously appearing in the literature, yields a geometric realization of all the vertex operator realizations of the basic representation.