IICKHO SONG, Korea Advanced Institute of Science and Technology An Extension of the Vandermonde Convolution Formula

As an extension of the Vandermonde Convolution $\sum_{m=0}^{\gamma} {\binom{\alpha}{\gamma-m}} {\binom{\beta}{m}} = {\binom{\alpha+\beta}{\gamma}}$, an explicit expression for the sum $\sum_{m=0}^{\gamma} m(m-1)\cdots(m-\zeta+1){\binom{\alpha}{\gamma-m}} {\binom{\beta}{m}}$ is obtained, where ${\binom{n}{r}} = \frac{n!}{(n-r)!r!}$ denotes the binomial coefficient. Some examples for the application of the result are considered.