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Tensor Products of Galois Representations

Let $\rho_{A_i, \ell} : G_K \rightarrow \text{Aut}(V_\ell(A_i))$ be the ℓ -adic Galois representation attached to an abelian variety A_i/K , and let $\tau_{A_i, \ell} : \text{End}(A_i) \otimes \mathbb{Q}_\ell \xrightarrow{\sim} \text{End}_{\mathbb{Q}_\ell[G_K]}(V_\ell(A_i))$ be the canonical isomorphism (Tate/Faltings). The purpose of this talk is to study properties of the tensor product $\rho_{A_1, \ell} \otimes \rho_{A_2, \ell}$ of two such representations, particularly in view of the following question: when is $\tau_{A_1, \ell} \otimes \tau_{A_2, \ell} : \text{End}(A_1) \otimes \text{End}(A_2) \otimes \mathbb{Q}_\ell \rightarrow \text{End}_{\mathbb{Q}_\ell[G_K]}(V_\ell(A_1) \otimes V_\ell(A_2))$ an isomorphism? (This question is related to Tate's Conjecture for codimension 2 cycles on products of abelian varieties.) In this talk I will give a solution in the case when $K = \mathbb{Q}$ and $A_i = A_{f_i}$ is a modular abelian variety attached to a weight 2 newform f_i on $\Gamma_1(N_i)$. If time permits, I will also discuss mod ℓ analogues.