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*Nonvanishing mod  $p$  of Eisenstein series*

Ribet's idea about the congruence argument between automorphic forms turns out to be useful in the proof towards one direction of Iwasawa main conjecture. In the proof, a  $p$ -integral Eisenstein series  $E$  needs to be constructed so that  $E \not\equiv 0 \pmod{p}$ . I will recall in several cases ( $\mathrm{GSp}(4)$  by Urban and  $U(2, 1)$  by Mainardi), how this problem was solved, then explain the difficulty of obtaining such result for an Eisenstein series on  $U(3, 1)$ . At last, I will show the result we have so far through the calculation of Fourier–Jacobi coefficient of this Eisenstein series.