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A conjectural uniform construction of many rigid Calabi-Yau threefolds

Given a rational Hecke eigenform f of weight 2, Eichler-Shimura theory gives a construction of an elliptic curve over \mathbb{Q} whose associated modular form is f. Mazur, van Straten, and others have asked whether there is an analogous construction for Hecke eigenforms f of weight k > 2 that produces a variety for which the Galois representation on its etale H^{k-1} (modulo classes of cycles if k is odd) is that of f. In weight 3 this is understood by work of Elkies and Schütt, but in higher weight it remains mysterious, despite many examples in weight 4. In this talk I will present a new construction based on families of K3 surfaces of Picard number 19 that recovers many existing examples in weight 4 and produces almost 20 new ones.