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Selberg's Central limit theorem for quadratic Dirichlet L-functions over function fields

In this talk we will discuss the logarithm of the central value $L\left(\frac{1}{2}, \chi_D\right)$ in the symplectic family of Dirichlet L -functions associated with the hyperelliptic curve of genus g over a fixed finite field \mathbb{F}_q in the limit as $g \rightarrow \infty$. Unconditionally, we show that the distribution of $\log |L\left(\frac{1}{2}, \chi_D\right)|$ is asymptotically bounded above by the full Gaussian distribution of mean $\frac{1}{2} \log \deg(D)$ and variance $\log \deg(D)$, and also $\log |L\left(\frac{1}{2}, \chi_D\right)|$ is at least 94.27% Gaussian distributed. Assuming a mild condition on the distribution of the low-lying zeros in this family, we obtain the full Gaussian distribution.