
RACHEL OLLIVIER, UBC

The pro-p-Iwahori Hecke Ext-algebra of $SL(2, \mathbb{Q}_p)$

Given a p-adic reductive group G and its (pro-p) Iwahori-Hecke algebra H , we are interested in the link between the category of smooth representations of G and the category of H -modules. When the field of coefficients has characteristic zero this link is well understood by work of Bernstein and Borel.

In characteristic p things are still poorly understood and the role of the pro-p Iwahori-Hecke algebra H is played by a differential graded Hecke algebra. In particular, by work of Peter Schneider, the module category over the d.g. Hecke algebra is equivalent to the derived category of smooth representations of G . Unlike in the case of H , we know little about the structure of this d.g. Hecke algebra.

In this talk I will report on joint work with Peter Schneider where we study the cohomology of the d.g. Hecke algebra. When $G = SL(2, \mathbb{Q}_p)$ we now understand its structure well enough to deduce some properties of mod p representations of $SL(2, \mathbb{Q}_p)$. We also have results for certain more general groups.