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Partial ordinary, and bumpless, pipe dreams

First I'll define "partial pipe dreams", which is somewhere between a permutation and a pipe dream for that permutation. To each such D I'll associate a variety $Y_D \subseteq \text{Mat}_n$ that is correspondingly between a matrix Schubert variety and a coordinate subspace. Then the inductive theorem is that if we revlex the matrix variable at an "outer corner" (i, j) of D , Y_D degenerates to a union of various $Y_{D'}$ where the pipe dream part of D' is that of D plus one more tile at (i, j) . Then I'll talk about the projective dual statement, lexing partial bumpless pipe dreams. Time permitting, I'll talk about joint work in progress with P. Zinn-Justin interpolating between the ordinary and bumpless pictures.