

---

**MURRAY R. BREMNER**, University of Saskatchewan

*Computing a short basis for the nullspace of a modular matrix*

Given a vector  $X$  over the field with  $p$  elements, define its length to be the sum of the squares of the symmetric representatives of its components. Define the length of a finite set of vectors to be the base 10 logarithm of the product of the lengths of the vectors. I will present an evolutionary algorithm which attempts to determine the shortest basis of the nullspace of a modular matrix  $A$ . To begin, compute  $M$ , the matrix in RREF whose  $k$  rows form a basis for the null space of  $A$ . One generation consists of six steps. Step 1 (mutation): Randomly permute the columns of  $A$  to obtain  $B$ . Step 2: Compute  $C$ , the matrix in RREF whose  $k$  rows form a basis for the null space of  $B$ . Step 3: Unpermute the columns of  $C$  to obtain  $N$ . Step 4 (recombination): Stack  $M$  and  $N$  and sort the  $2k$  rows by increasing length to obtain  $D$ . Step 5 (selection): Determine the lexicographically minimal subset of the rows of  $D$  which forms a basis of the nullspace of  $A$ . Step 6 (reproduction): Replace  $M$  by the matrix consisting of these  $k$  rows of  $D$ . I will present experimental results showing the behavior of this algorithm over thousands of generations.