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Symmetric products of maximal varieties

Let X be a complex algebraic variety equipped with an antiholomorphic involution τ . Then the mod 2 Betti sum of the real part X^τ cannot exceed the mod 2 Betti sum of X . In case of equality one calls X *maximal* or an *M-variety*. Biswas–D’Mello have shown that if a compact connected Riemann surface, say of genus g , is maximal, then so is its n -th symmetric power for $n \leq 3$ and $n \geq 2g - 1$. We show that this holds for any n . As we will explain, this is actually a purely topological statement about symmetric products and, more generally, Γ -products of equivariantly formal spaces.