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Simultaneous torsion points in a Weierstrass family of elliptic curves
In 2010, Masser and Zannier proved that there are at most finitely many complex numbers $t$, not equaling 0 or 1 , such that the two points on the Legendre elliptic curve $y^{2}=x(x-1)(x-t)$ with $x$-coordinates 2 and 3 are simultaneously torsion. Recently, Stoll proved that there is in fact no such $t$, and it is his result that inspires our work. In this talk we will focus on the Weierstrass family of elliptic curves $E_{t}: y^{2}=x^{3}+t$, and show that in many instances there is no parameter $t$ such that the points $(a, *)$ and $(b, *)$ are simultaneously torsion in $E_{t}$. In contrast to the original approach of Masser and Zannier, our approach is dynamical. We focus on studying whether $a$ and $b$ are simultaneously preperiodic for a Lattès map.

