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*The Topology of Representation Spaces*

Let  $\Gamma$  be a finitely generated group and let  $G$  be a reductive complex linear algebraic group (e.g.  $SL_n\mathbb{C}$ ). The representation space  $\text{Hom}(\Gamma, G)$  carved out of a finite product of copies of  $G$  by the relations of  $\Gamma$  has many interesting topological features. From the point of view of algebraic topology, these features are easier to understand for the compact subspace  $\text{Hom}(\Gamma, K) \subset \text{Hom}(\Gamma, G)$  where  $K$  is a maximal compact subgroup of  $G$  (e.g.  $SU_n$ ). Unfortunately, the topological spaces  $\text{Hom}(\Gamma, G)$  and  $\text{Hom}(\Gamma, K)$  usually have very little to do with each other; for instance, some of the connected components of  $\text{Hom}(\Gamma, G)$  may not even intersect  $\text{Hom}(\Gamma, K)$ ! In this talk, I will discuss exceptional classes of groups  $\Gamma$  for which  $\text{Hom}(\Gamma, G)$  and  $\text{Hom}(\Gamma, K)$  happen to be homotopy equivalent, thereby allowing one to compute otherwise inaccessible topological invariants.