KEVIN HARE, University of Waterloo
Simultaneous beta-expansions
We say that $x$ has a beta-expansion with respect to $\beta$ if there exists a sequence of $a_{i}$ such that $x=\sum a_{i} \beta^{-i}$. It is known that if $\beta>1$ is sufficiently close to 1 , and the digits $a_{i}$ are restricted to $\pm 1$ then all $x$ sufficiently close to 0 have an uncountable number of beta-expansions.
What is surprising is that for any $x_{1}$ and $x_{1}$ sufficiently close to 0 and $\beta_{1} \neq \beta_{2}$ sufficiently close to 1 we can find a beta-expansion that is simultaneously a beta-expansion for $x_{1}$ in terms of $\beta_{1}$ and is a beta-expansion for $x_{2}$ in terms of $\beta_{2}$.
We will discuss the proof of this result, the generalization of this to higher numbers of simultaneous beta-expansions, and the limits of these techniques.

