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Definability of algebraic models

By a theorem of Akbulut and King, every smooth compactifiable manifold N (that is, N is diffeomorphic to the interior of a smooth compact manifold with boundary) is diffeomorphic to a non-singular real algebraic set. We say that N admits an algebraic model. We discuss the definability of the diffeomorphism under the assumption that the underlying set of N is definable in an expansion of the real field. In general, every definably compactifiable differentiable (C^k for finite k) manifold admits definably an algebraic model. For structures expanding the real exponential field we obtain stronger results. There, definably compactifiable smooth manifolds admit definably and smooth algebraic models.