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*A proper reduct of the real projective hierarchy that defines sets in each projective level*

There exist closed  $E \subseteq \mathbb{R}$  such that  $(\mathbb{R}, +, \cdot, E)$  defines a Borel isomorph of  $(\mathbb{R}, +, \cdot, \mathbb{N})$ , and so defines sets of every projective level, yet does not define  $\mathbb{N}$ , even when  $(\mathbb{R}, +, \cdot, E)$  is further expanded by all subsets of every cartesian power of  $E$ .

Joint work with Harvey Friedman.