
QIAN WANG, University of Alberta
Some Results On A Diffusive SIR Model

The model we are interested in is given by

$$\begin{cases} S_t = d_1 S_{xx} + \Lambda - \beta(x)IS - b_1 S, \\ I_t = d_2 I_{xx} + \beta(x)IS - (b_2 + \gamma)I, \\ R_t = d_3 R_{xx} + \gamma I - b_3 R, \end{cases} \quad 0 < x < 1, t > 0 \quad (1)$$

with homogeneous Neumann boundary conditions, where S , I , R denote the number of susceptible, infectious and recovered population, respectively. In this talk, I will present some results on the existence and the structure of global attractor, and the existence of positive steady states. We prove that there exists a threshold parameter R_0 , whose sign determines the structure of the global attractor. If $R_0 \leq 0$, the disease-free equilibrium P_0 is globally stable. If $R_0 > 0$, P_0 is unstable, and a positive, x -dependent endemic equilibrium P^* exists. In the special case when $\beta(x) = \text{constant}$, P^* is independent of x and is globally stable.

This is a joint work with Michael Y. Li.